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DEPARTMENT OF OCEAN ENGINEERING

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LAMINAR FLOW HEAT EXCHANGERS -
VISCOSITY INDUCED NON-UNIFORM FLOW

by

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Ocean Eng.
S.M. in M.E.

June, 1984
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VISCOSITY INDUCED NON-UNIFORM FLOW

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LAMINAR FLOW HEAT EXCHANGERS -
VISCOSITY INDUCED NON-UNIFORM FLOW

by

GREER REED PUTNAM

Submitted to the Department of Ocean Engineering on May 11, 1984, in partial fulfillment of the requirements for the Degrees of Ocean Engineer and Master of Science in Mechanical Engineering.

ABSTRACT

Laminar flow heat exchangers which cool oil in non-inter-connected parallel passages can experience non-uniform flows and a reduction in the effective heat exchanger coefficient in a range of Reynolds number which varies with tube length and diameter, tube wall temperature and fluid inlet temperature. The method of predicting the reduction in effective heat transfer coefficient and the range of Reynolds number over which these instabilities exist is presented for a particular oil, Mobil aviation oil 120. Included, also, is the prediction of the effect of radial viscosity variation on the constant property magnitudes of friction and heat transfer coefficient.

Thesis Supervisor: Professor Warren M. Rohsenow

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INTRODUCTION

Heat exchangers that operate in the laminar flow regime with non-interconnected parallel passages can depart from predicted performance as a result of non-uniform flow distributions. Variations in the flow distribution among the tubes can be caused by the effect of the fluid viscosity/temperature relation, natural convection and non-uniform passage sizes (from design and manufacturing tolerances). If the exchanger is oriented vertically with the colder side up, the effect of natural convection can be eliminated. Non-uniform passage size can be minimized through quality control. Therefore, the effect of the viscosity/temperature relation on non-uniform flow will be analyzed in this paper.

The viscosity/temperature relation for the Mobil aviation oil 120 used in this analysis is presented in Fig. 1. Viscosity is a strong function of temperature, decreasing as temperature increases. In this analysis it is assumed that other fluid properties such as density and thermal conductivity are uniform at $\rho = 55.0 \text{ lbm/ft}^3$ (881.0 kg/m^3), $k = 0.08 \text{ BTU/hr}\cdot\text{ft}\cdot\text{F}$ ($0.138 \text{ W/m}\cdot\text{C}$) and $c_p = 0.5 \text{ BTU/lbm}\cdot\text{F}$ ($2.09 \times 10^3 \text{ J/kg}\cdot\text{C}$). This is a reasonable assumption for oils. Also, it is assumed that pressure drop entrance and exit effects can be neglected. The analysis was performed for flow in tubes. Uniform wall temperature was assumed assuming the heat transfer coefficient was very much greater on the outside than on the inside of the tube.

When cooling liquids or heating gases, non-uniform flow can exist in the flow passages. For the same overall pressure drop, two

discrete flow rates can exist in the same heat exchanger.

This problem has been discussed by Mueller [1], [2] and [3] and Rohsenow [4].

EFFECT OF RADIAL VISCOSITY VARIATION

The fully developed fluid and temperature distributions in a tube are non-parabolic due to the viscosity/temperature relation. This causes a lower velocity of the colder fluid near the tube wall and a higher velocity of the hotter fluid near the centerline compared with the constant property case (ie. uniform viscosity) with the same flow rate and bulk temperature.

For steady state, fully developed flow and viscosity as a function of temperature, the momentum equation reduces to:

$$\frac{dp}{dx} = \frac{1}{r} \frac{\partial}{\partial r} \left(r \mu \frac{\partial u}{\partial r} \right) \quad (1)$$

Neglecting the effects of axial conduction and assuming constant heat flux at the tube wall, the temperature distribution for fully developed conditions is:

$$r k \frac{\partial T}{\partial r} = \frac{d}{dx} \int \rho c_p u T r dr \quad (2)$$

An expression is needed to account for the change in friction factor and Nusselt number for the variable properties case (ie. variable viscosity) compared with the constant properties case (ie. uniform

viscosity). Assume that the effect can be expressed as the ratio of the wall to bulk viscosities raised to an exponent as follows:

$$\frac{f}{f_{c_p}} = \left(\frac{\mu_o}{\mu_b} \right)^m \quad (3)$$

$$\frac{Nu}{Nu_{c_p}} = \left(\frac{\mu_o}{\mu_b} \right)^n \quad (4)$$

f_{c_p} and Nu_{c_p} are based on constant properties at the bulk temperature.

To find exponents m and n , Eqs. (1) and (2) were solved simultaneously using an iterative procedure. An average fluid velocity, wall temperature and parabolic temperature distribution were assumed initially. The fluid viscosity versus temperature relation of Fig. 1 was closely approximated by a piecewise curve fit using a sixth degree polynomial. Based on the assumed temperature distribution, the viscosity $\mu(r)$ was determined. Equation (1) was solved for the fluid velocity based on the viscosity $\mu(r)$. The dp/dx term was adjusted to obtain the desired average fluid velocity. Next, the temperature distribution from Eq. (2) was determined using the calculated fluid velocity. Then, the friction factor and Nusselt number were calculated. The viscosity $\mu(r)$ was determined for the revised temperature distribution and the procedure was repeated until the calculated friction factors and Nusselt numbers agreed within less than 1%.

The results of this analysis showed that the exponents m and

n varied as a function of wall and bulk temperature as shown in Figs. 2 and 3. The exponents were invariant to changes in the average fluid velocity.

SINGLE TUBE PRESSURE DROP

Having quantified the radial effects of the viscosity/temperature relation on friction factor and Nusselt number using the ratio of the wall to bulk viscosities and the exponents m and n , an analysis is performed on a heat exchanger tube. An energy balance at the tube wall for uniform wall temperature yields:

$$w c_p dT = h\pi D(T - T_o)dx \quad (5)$$

or

$$\frac{dT}{T-T_o} = \frac{\pi k}{w c_p} \left(\frac{hD}{k} \right) dx \quad (6)$$

Preliminary calculations showed that the fluid flow was fully developed a short distance from the tube entrance and entrance effects could be neglected. However, entrance effects on the temperature distribution had to be taken into account because of the slowly developing temperature distribution. The following equation was suggested by Kays [5] to account for variation in the Nusselt number in the entrance region of tubes for uniform wall temperature:

$$Nu = 3.66 + \frac{0.0668 \frac{4}{\pi x} \frac{w c_p}{k}}{1 + 0.04 \left[\frac{4}{\pi x} \frac{w c_p}{k} \right]^{2/3}} \quad (7)$$

Therefore, the equation to determine the temperature drop along the heat exchanger is given by combining Eqs. (4), (6) and (7):

$$\frac{\Delta T}{T - T_o} = \left(\frac{\mu_o}{\mu_b} \right)^n \left(3.66 + \frac{0.0668 \frac{4}{\pi x} \frac{w_c p}{k}}{1 + 0.04 \left[\frac{4}{\pi x} \frac{w_c p}{k} \right]^{2/3}} \right) \frac{\pi k}{w_c p} \Delta x \quad (8)$$

Equation (8) includes the radial effects and the developing temperature distribution effects. The temperature change along the tube was solved by iteration of values of bulk viscosity, local temperature and exponent n . The temperature change and bulk viscosity along the tube for various flow rates is shown in Figs. 4 and 5 for a 0.25" diameter tube and tube wall temperature of 40 F.

It can be shown that the pressure drop for an increment dx along a tube is given by:

$$\frac{dp}{dx} = \frac{64}{Re} \frac{1}{D} \frac{G^2}{2\rho} \quad (9)$$

Equation (9) is multiplied by Eq. (3) to account for radial effects on the friction factor.

$$\frac{dp}{dx} = \frac{64}{Re_b} \left(\frac{\mu_o}{\mu_b} \right)^m \frac{1}{D} \frac{G^2}{2\rho} \quad (10)$$

In integral form Eq. (10) becomes:

$$\Delta P = \frac{128}{\pi \rho D^4} w \int_0^L \mu_o^m \mu_b^{1-m} dx \quad (11)$$

The curves of pressure drop versus flow rate for various lengths of tube were calculated (Fig. 6) for $D = 0.25''$, $T_o = 40$ F and $T_i = 300$ F. It is observed that ΔP goes through a maximum, then a minimum, followed by a continuous rise as the flow rate is increased. From Eq. (11), $\Delta P \sim D^{-4}$; therefore ΔP vs. w curves for other tube diameters would look like those of Fig. 6 but be displaced vertically proportional to D^{-4} .

MULTI-TUBE HEAT EXCHANGER PERFORMANCE

These curves are for single tubes but may be used to predict the flow maldistribution and resulting effective Nusselt number for multi-tube heat exchangers. This exchanger performance is determined by how the total flow is supplied - constant flow pump (gear pump), constant head source or variable head-flow pump (centrifugal pump).

a) Constant Flow Pump

In the case of a heat exchanger with five tubes ($L = 4'$, $D = 0.25''$), non-uniform flow can exist as shown in Fig. 7. For an inlet flow rate of 25.75 lbm/hr (average flow rate of 5.15 lbm/hr per tube) and inlet temperature of 300 F and wall temperature of 40 F, four of the tubes have a flow rate of 1.26 lbm/hr with an exit temperature of 42.7 F and one tube has a higher flow rate of 20.7 lbm/hr

with an exit temperature of 220.0 F. The average bulk temperature at the exchanger outlet is 185.2 F. Figure 8 shows a plot of temperature along the exchanger for one tube at higher flow and four tubes with lower flow. The average exit temperature (T_{avg}) is the summation of the individual tube exit temperature weighted by the percentage of flow through each tube. This is the temperature that would be measured at the heat exchanger exit after mixing the five streams. If it were not known that this maldistribution existed and it were assumed that the flow was uniform in the five tubes at one-fifth of the total flow, the effective Nusselt number would be determined using T_{avg} as follows:

$$Nu_{eff} = \frac{h_{eff} D}{k} \quad (12)$$

$$h_{eff} = \frac{c_p W}{n_o \pi D L} \log \left(\frac{T_o - T_i}{T_o - T_{avg}} \right)$$

For this case $h_{eff} = 5.72 \text{ BTU/hr}\cdot\text{ft}^2\cdot\text{F}$ ($32.49 \text{ W/m}^2\cdot\text{C}$) and $Nu_{eff} = 1.49$. Also shown in Fig. 8 is the temperature along the exchanger and the exit temperature ($T_{uniform}$) if the tubes, in fact, had uniform flow. For this case $h_{eff} = 10.37 \text{ BTU/hr}\cdot\text{ft}^2\cdot\text{F}$ ($58.87 \text{ W/m}^2\cdot\text{C}$) and $Nu_{eff} = 2.70$. Since $T_{avg} > T_{uniform}$, the Nusselt number (and heat exchanger performance) is lower when non-uniform flows exist.

An enlarged view of the region of non-uniform flows is shown in Fig. 9. On Fig. 9 curve (c-d) at any ΔP level represents the

average flow rate with four tubes having a flow rate on curve (u-a) and one tube on curve (m-l), the stable flow curves. Then $5w_{cd} = 4w_{ua} + w_{ml}$. Curves (s-f), (g-h) and (o-j) are similar curves for flow splits of 3-2, 2-3 and 1-4 tubes on curves (u-a) and (m-l). As the total flow rate is increased, uniform flow exists through the peak at point(a) and on to point (b). At point (b) the pressure drop decreases suddenly to point (c) where one tube has a higher flow rate while the other four tubes have lower flow rates. The total flow rate is: $5w_b = 5w_c = 4w_u + w_m$. As flow is further increased, flow increases in each of the tubes (along the pressure drop curve) with the average flow rate shown as line (c-d). Point (d) is the point depicted in Figs. 7 and 8. As flow is increased slightly above the flow corresponding to point (d), the pressure drop falls from points (d) to (e) and now two tubes have higher flow rates and three tubes have lower flow rates. As the flow is increased, the flow in each tube increases with the average flow rate shown on the line (e-f). This process continues until uniform flow in all five tubes occurs at point (k). In the case of infinite tubes, the average flow rate would follow the line (a-l) with flow in the tubes corresponding to the flow at either point (a) - (lower flow rate) - (l) - (higher flow rate). The mix of tubes with higher and lower flow rates is determined by the average fluid flow rate.

For the case of decreasing flow rate, non-uniform flows also occur. As flow is decreased to point (m) the pressure drop decreases with all tubes having uniform flow. The pressure drop suddenly increases from points (m) to (n) at which one tube has lower flow and

four tubes have higher flow. As flow is decreased further, flow in each tube decreases with the average flow rate given by line (n-o). Additional tubes "pop-over" to lower flow at points (o), (q), (s) and (c). All the tubes have the same flow rate at point (b). In the case of infinite tubes the average flow rate would follow line (m-u) with flow in the tubes corresponding to the flow at either point (u) - lower flow rate - or (m) - higher flow rate.

Figure 10 shows the effects of non-uniform flow on the Nusselt number as a function of Reynolds number for the case of five tubes. The solid line is for increasing flow and the dashed line is for decreasing flow. The Nusselt number is reduced significantly between points (b) and (k) for increasing flow and between points (m) and (b) for decreasing flow. These are the regions of the curve where non-uniform flow exists.

For the case of infinite tubes, the effect of non-uniform flow on exchanger performance is shown in Figs. 11 and 12. As the tube diameter is decreased, the region of non-uniform flow is extended to higher Reynolds numbers but the Nusselt number decreases less. Increasing the tube length has an effect on exchanger performance similar to that of decreasing the tube diameter.

b) Constant Head Source

For the constant head source, as the pressure drop is increased beyond point (a) of Fig. 9, the average flow rate will increase to point (1) regardless of the number of tubes. With con-

tinual increase in constant head, operation can not be sustained at flow rates between points (a) and (1). For the case of continual decreasing constant head, all tubes remain operating along line (1) to (m). Then the flow drops to point (u) in all tubes.

c) Variable Head-Flow Pump

For a centrifugal pump source with the pump characteristic shown as lines (a-b) and (c-d) in Fig. 13, non-uniform flows can also exist. The situation is much the same as for the case of a constant head source except that the average flow follows the pump characteristic instead of the constant head line. As pump speed is increased above the point (a) all tubes shift to operation at point (b). The exchanger can not operate between points (a) and (b) at the higher speed nor between points (c) and (d) at the lower speed.

DISCUSSION

Variations in the tube wall and inlet temperature can affect the values of exponents m and n (Figs. 2 and 3). Together with the μ vs. T relation (Fig. 1), changes in exponents m and n can cause differences in the shape of the ΔP vs. w curve determined by Eq. (11). The ΔP vs. w curves for a single tube ($L = 4'$, $D = 0.25''$) are plotted in Fig. 14 for different combinations of wall and inlet temperature. The tube with $T_o = 40^\circ\text{F}$ and $T_i = 300^\circ\text{F}$ exhibits a region in which non-uniform flow can exist. If T_i is

changed from 300°F to 200°F, there is only a slight dip in the curve and the region of non-uniform flow is narrower. If T_o is changed from 40°F to 100°F with $T_i = 300^\circ\text{F}$, no region of non-uniform flow exists.

Results were similar for calculations done using another oil, Mobil automotive oil HD-30.

CONCLUSIONS

Laminar flow, parallel passage heat exchangers can experience maldistribution of flow and a reduction in the effective heat transfer coefficient in a range of Reynolds number which varies with length, tube diameter and the levels of the temperature - wall and inlet.

For Mobil aviation oil 120 with the μ vs. T relation of Fig. 1, the exponents m and n in the viscosity correction ratios, Eqs. (3) and (4), are shown to vary with both wall and bulk temperatures, Figs. 2 and 3.

NOMENCLATURE

c_p	specific heat at constant pressure
D	tube diameter
f	friction factor (variable viscosity)
f_{c_p}	friction factor (uniform viscosity evaluated at the bulk temperature)
G	mass flow rate
h_{eff}	effective heat transfer coefficient
k	thermal conductivity
L	tube length
m	exponent for friction factor correction
n	exponent for Nusselt number correction
n_o	number of tubes
Nu_{eff}	effective Nusselt number (variable viscosity)
Nu	Nusselt number (variable viscosity)
Nu_{c_p}	Nusselt number (uniform viscosity at the bulk temperature)
P	pressure along the tube
ΔP	tube pressure drop
r	tube radius, radial direction
Re_b	Reynolds number evaluated at μ_b
T	temperature as function of r or x
T_{avg}	average exit temperature in non-uniform flow condition
T_b	bulk temperature
T_o	wall temperature

T_i	inlet temperature
T_{uniform}	average exit temperature for uniform flow condition
u	fluid velocity in x - direction
W	total flow rate
w	individual tube flow rate
x	direction along tube

Greek Symbols

ρ	fluid density
μ	viscosity as function of T
μ_o	viscosity evaluated at T_o
μ_b	viscosity evaluated at T_b

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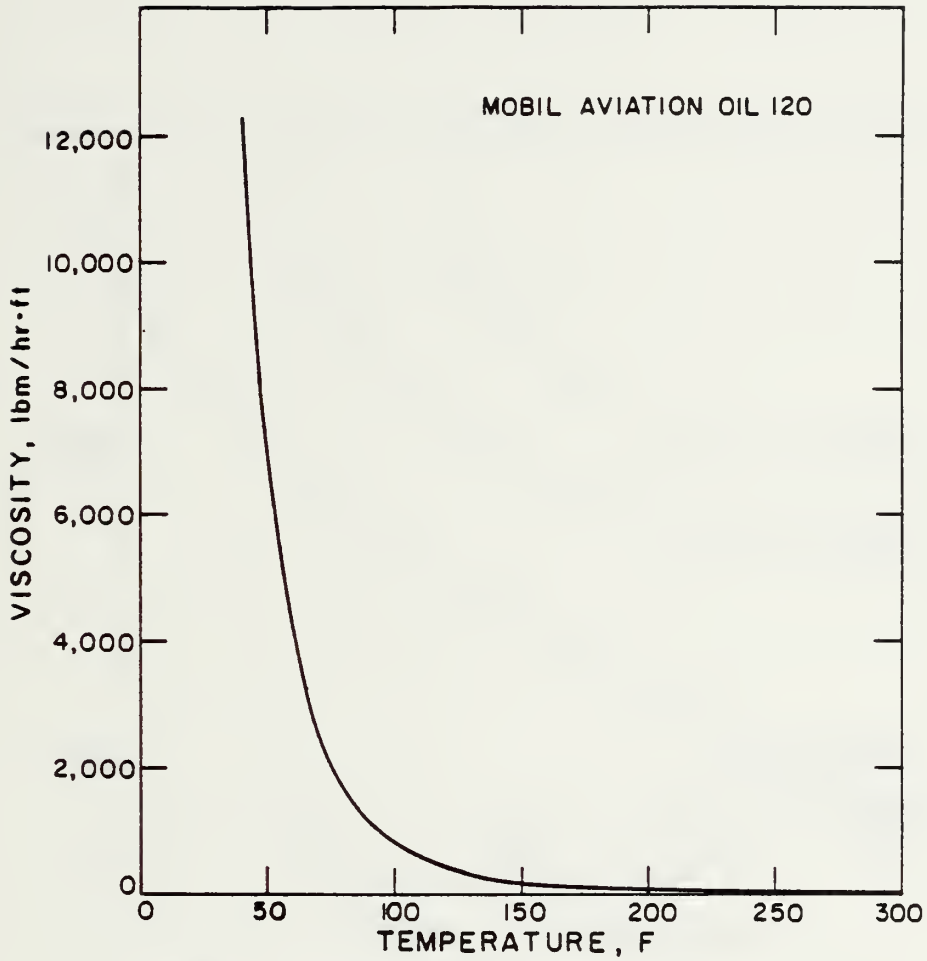
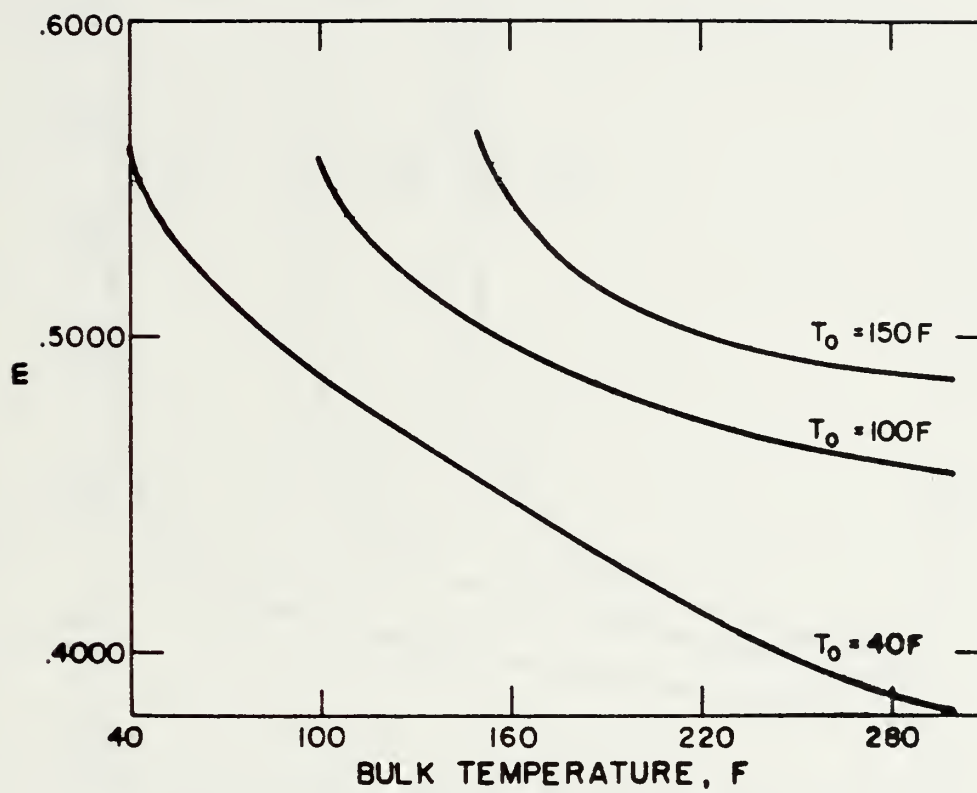
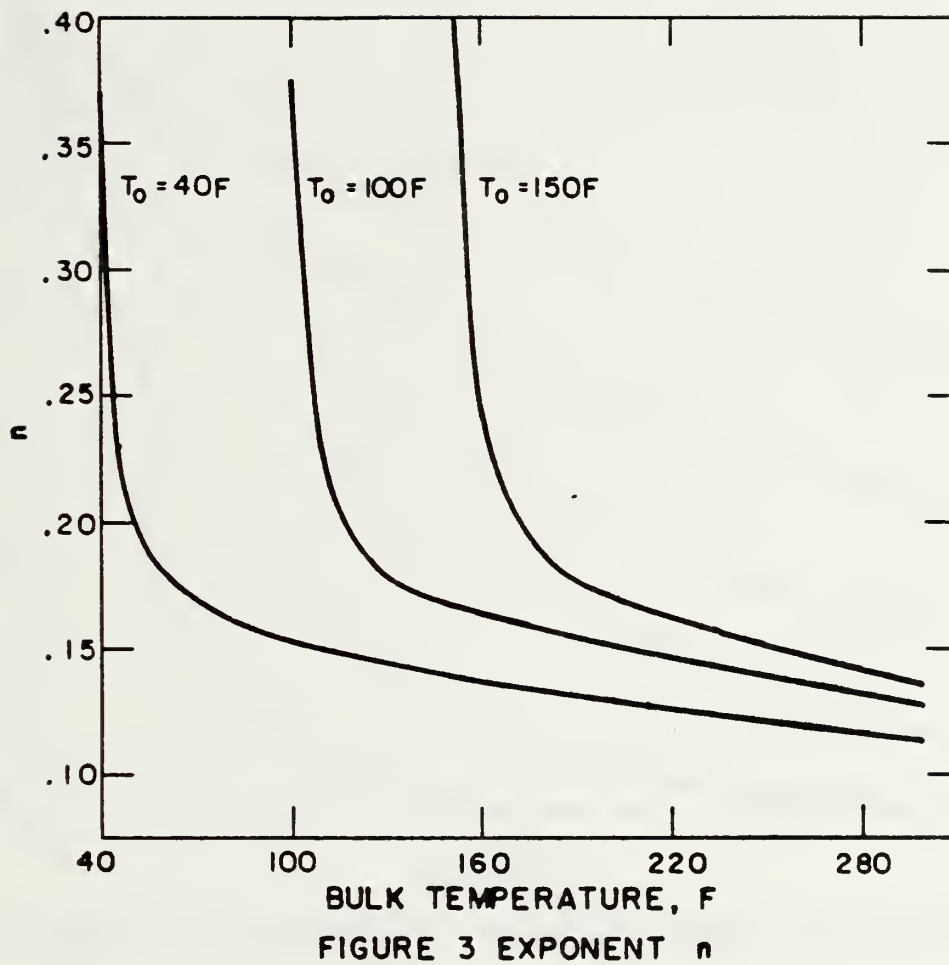


FIGURE 1 VISCOSITY VS TEMPERATURE RELATION

FIGURE 2 EXPONENT m



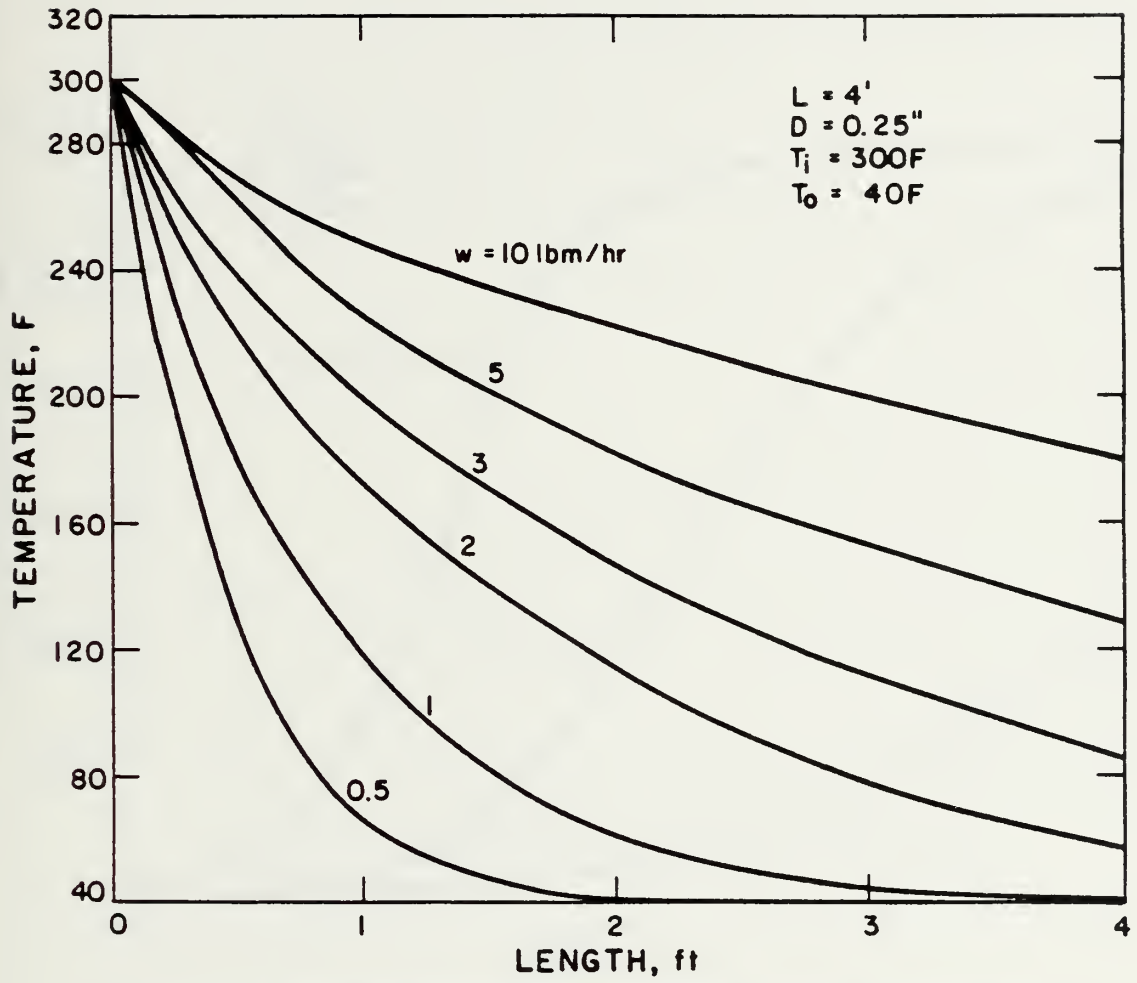


FIGURE 4 TEMPERATURE VARIATION ALONG EXCHANGER

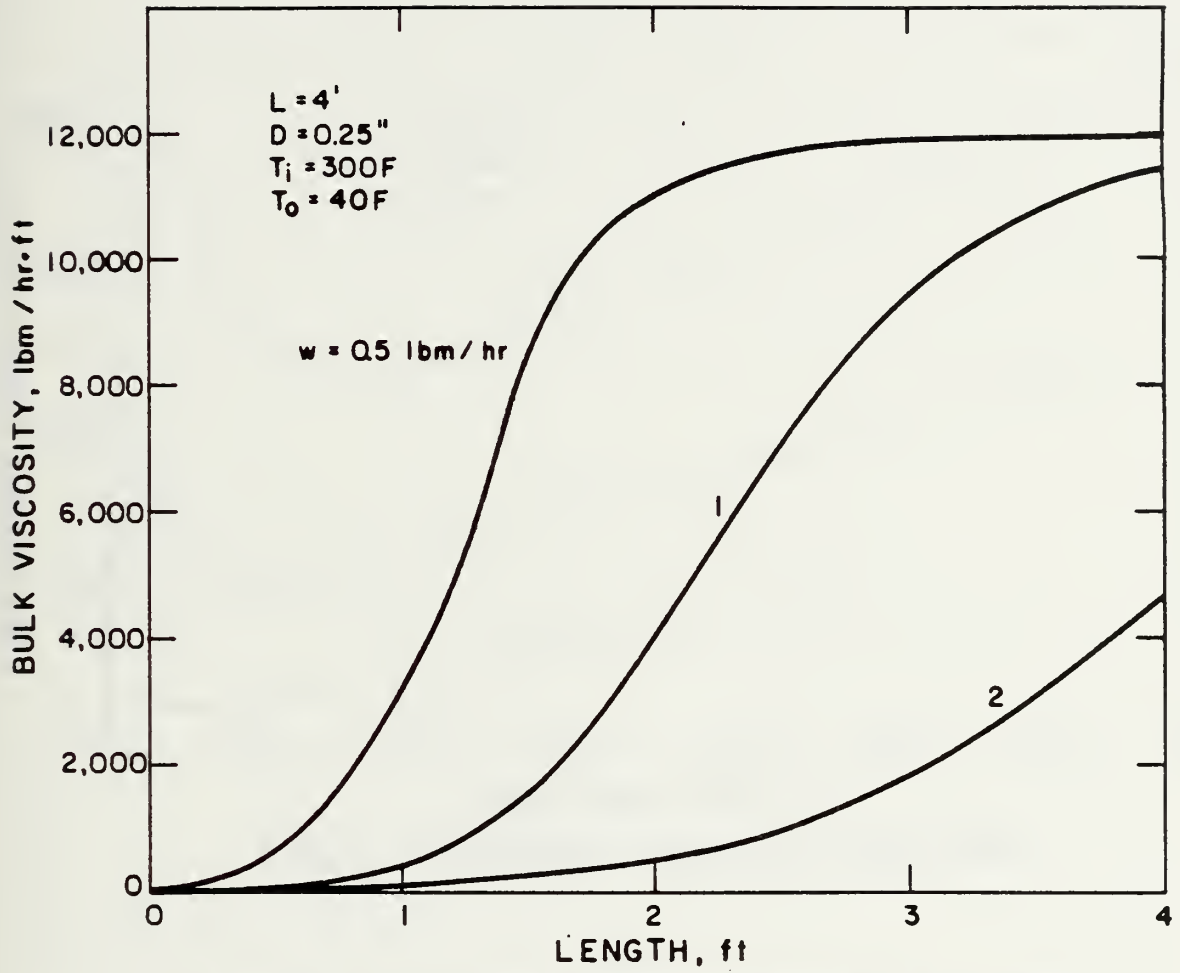


FIGURE 5 VISCOSITY VARIATION ALONG EXCHANGER

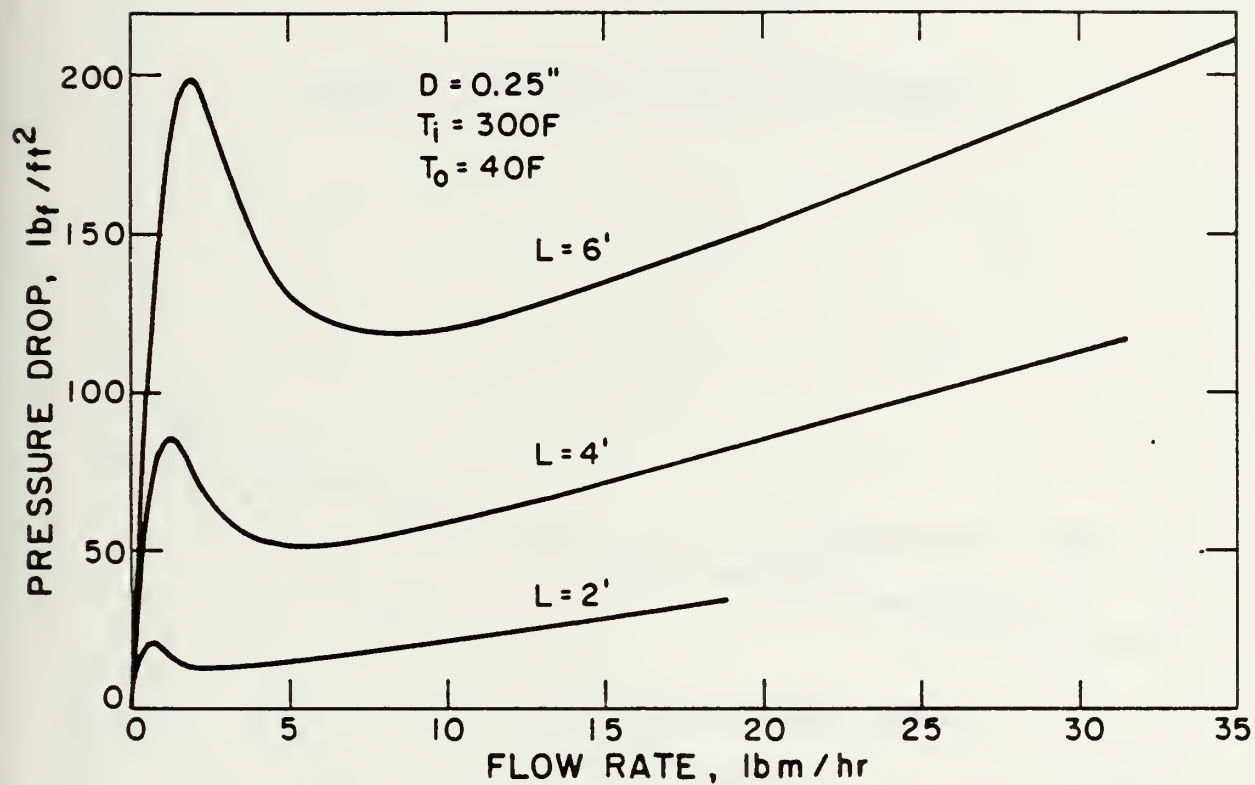


FIGURE 6 PRESSURE DROP VS. FLOW RATE

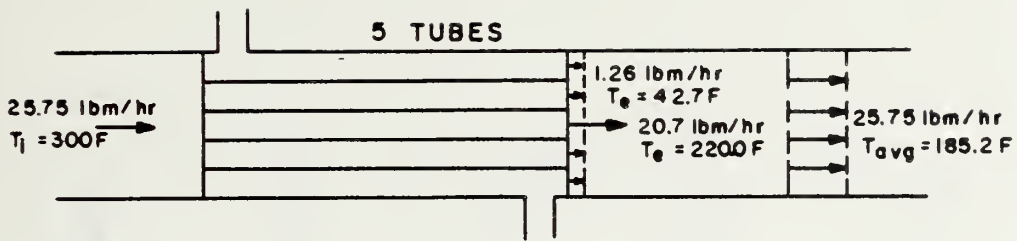


FIGURE 7 FIVE TUBE HEAT EXCHANGER

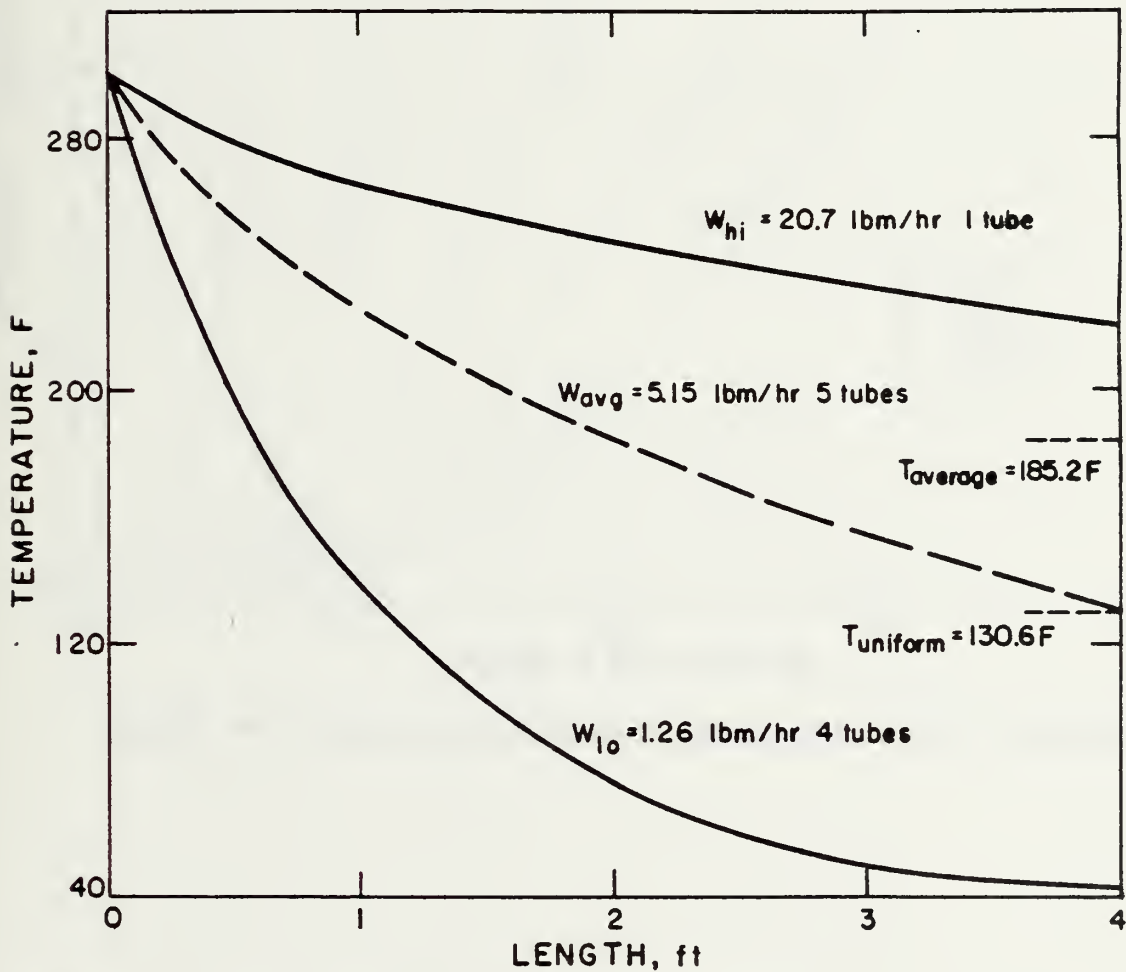


FIGURE 8 TEMPERATURE DISTRIBUTION FOR FIVE TUBE EXCHANGER

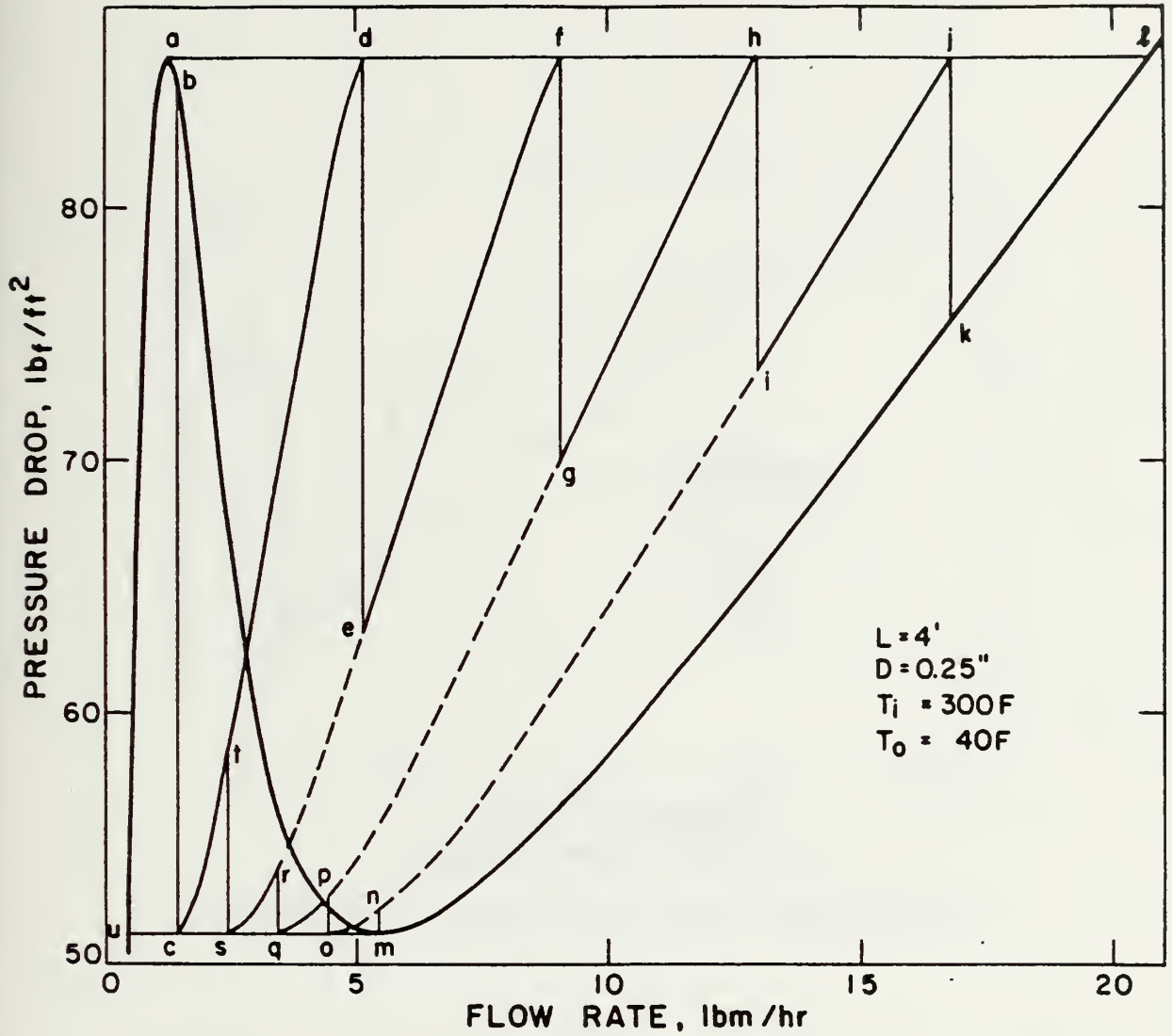


FIGURE 9 FLOW MALDISTRIBUTION IN FIVE TUBE EXCHANGER

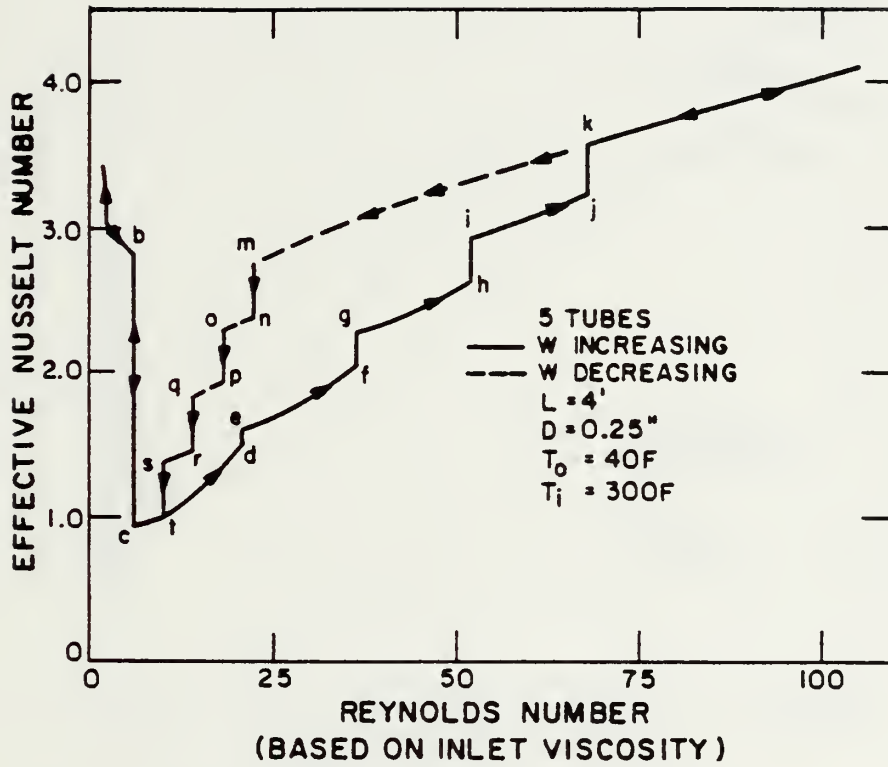


FIGURE 10 FIVE TUBE EXCHANGER PERFORMANCE

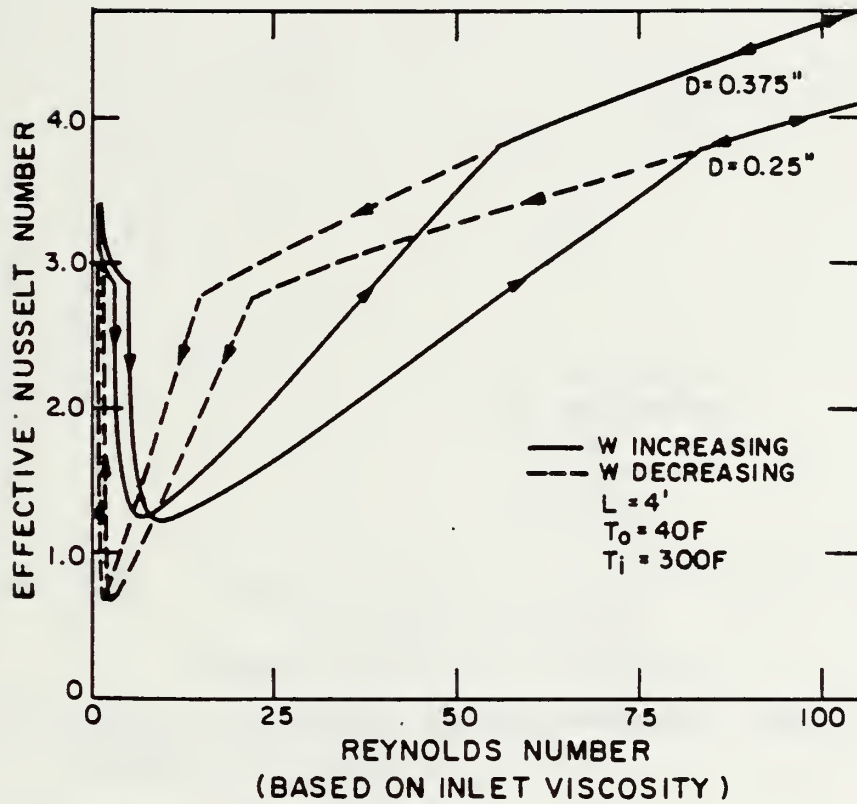


FIGURE II EFFECT OF DIAMETER ON PERFORMANCE
FOR AN INFINITE NUMBER OF TUBES

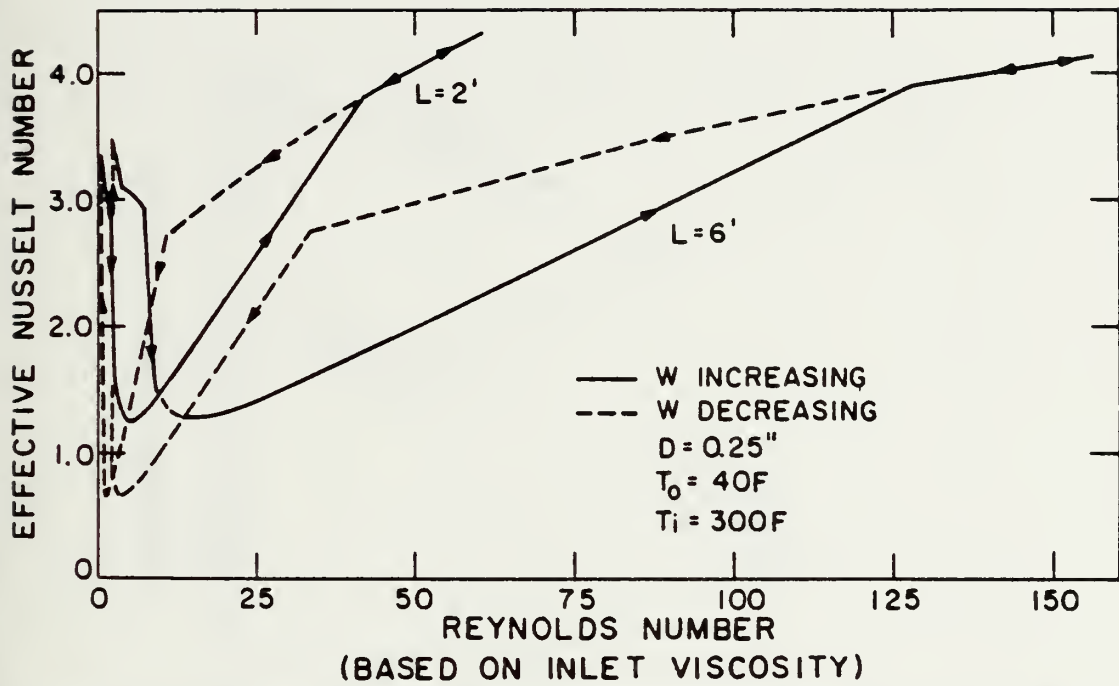


FIGURE 12 EFFECT OF LENGTH ON PERFORMANCE FOR AN INFINITE NUMBER OF TUBES

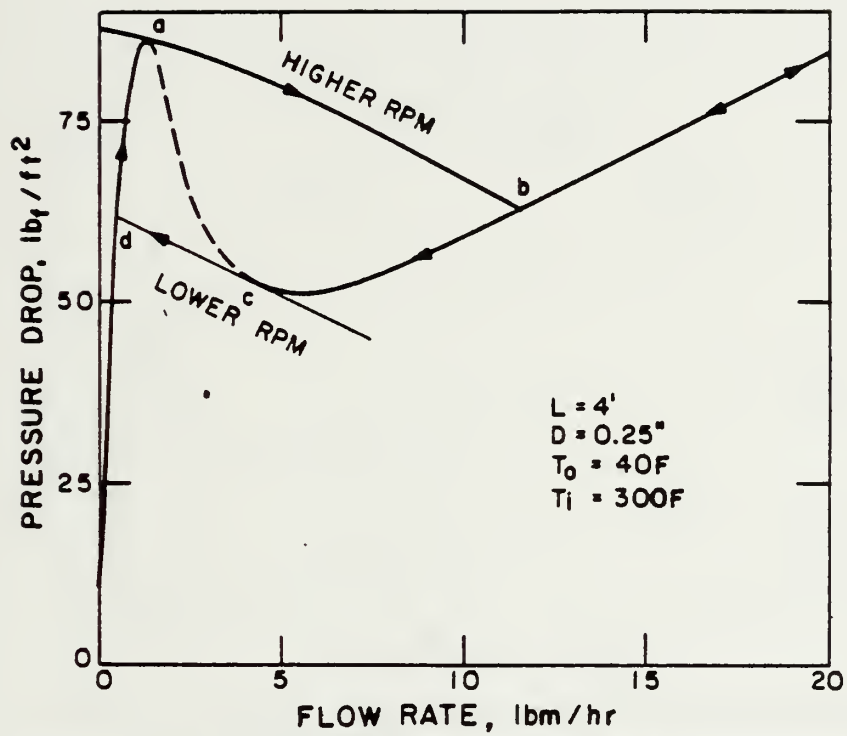


FIGURE 13 ΔP VERSUS W FOR VARIABLE HEAD-FLOW PUMP FOR INFINITE NUMBER OF TUBES

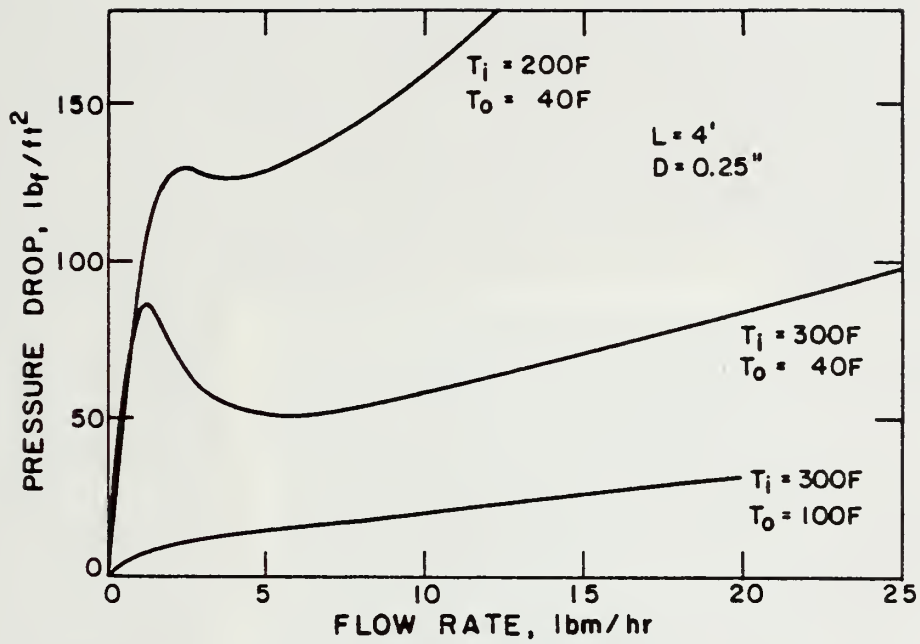


FIGURE 14 EFFECT OF TEMPERATURE LEVELS ON PRESSURE DROP CURVES

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